

## Chem 531: Problem Set #2

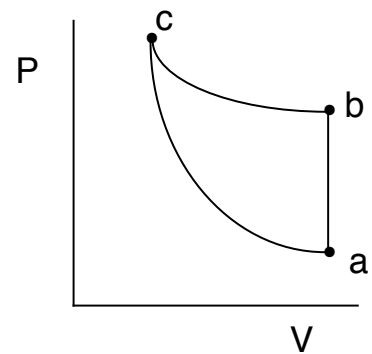
Due in class: Thurs, Sept. 14th

- (1) The heat capacities of a gas are often represented by expressions such as:

$$\bar{C}_p = \alpha + \beta T + \gamma T^2 + \delta T^3$$

For  $\text{N}_2$ ,  $\alpha = 28.883 \text{ J K}^{-1} \text{ mol}^{-1}$ ,  $\beta = -1.57 \times 10^{-3} \text{ J K}^{-2} \text{ mol}^{-1}$ ,  $\gamma = 0.808 \times 10^{-5} \text{ J K}^{-3} \text{ mol}^{-1}$ , and  $\delta = -2.871 \times 10^{-9} \text{ J K}^{-4} \text{ mol}^{-1}$ . How much heat is required to heat a mole of  $\text{N}_2$  from 200 to 1000 K at a constant pressure of 1 bar?

- (2) Compressing the system represented in the figure along the adiabatic path  $a \rightarrow c$  requires 1000 J of work. Compressing the system along the isothermal line  $b \rightarrow c$  requires 1500 J of work but 600 J of heat flows out of the system. Fill in the table below, paying close attention to signs.



Process	w	q	$\Delta U$
a $\rightarrow$ b			
b $\rightarrow$ c			
c $\rightarrow$ a			
cycle abca			

(3)

(a) Show that

$$\left(\frac{\partial C_v}{\partial V}\right)_T = T \left(\frac{\partial^2 P}{\partial T^2}\right)_V \quad \text{noting that} \quad \left(\frac{\partial U}{\partial V}\right)_T = T \left(\frac{\partial P}{\partial T}\right)_V - P$$

(b) Evaluate this for an ideal gas.

(4) The standard enthalpy of dissociation  $\Delta H_{diss}^o$  for hypobromous acid, i.e.,  $\Delta H_r^o$ , for the reaction  $\text{HOBr(g)} \rightarrow \text{OH(g)} + \text{Br(g)}$ , has been measured to be 206.8 kJ/mol at 25°C.

(a) Determine the standard internal energy change  $\Delta U_r^o$  for this reaction at 25°C.

(b) Determine the standard enthalpy of formation,  $\Delta H_f^o$ , of HOBr at 25°C [Note: you'll need to look up appropriate thermodynamic data for OH(g) and Br(g). See: <https://atct.anl.gov>]

(5) The standard enthalpy of combustion for liquid benzene at 25°C is -3268 kJ/mol. Determine the enthalpy of combustion of gaseous benzene at 110°C. Please note your sources for the required thermodynamic data.

(6) Two moles of superheated steam at 200°C is injected into 50 moles of 25°C water at a constant pressure of 1.0 bar under adiabatic conditions. Calculate the final temperature ( $T_f$ ) of the system. The constant pressure molar heat capacities of  $\text{H}_2\text{O(g)}$  and  $\text{H}_2\text{O(l)}$  are 33.6 and 75.3 J K<sup>-1</sup> mol<sup>-1</sup>, respectively, and can be assumed to be independent of temperature. The enthalpy of vaporization at 100°C and 1 bar for  $\text{H}_2\text{O}$  is 40.66 kJ mol<sup>-1</sup>.